

1 **EPIBLASTER-Fast exhaustive two-locus epistasis detection strategy using graphical**
2 **processing units.**

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43 **Running head:** EPIBLASTER fast GPU-based epistasis

44 **Keywords:** Epistasis, Genome-Wide Interaction Analysis, Graphical Processing Unit.

1 **Abstract**

2 Detection of epistatic interaction between loci has been postulated to provide a more in-
3 depth understanding of the complex biological and biochemical pathways underlying
4 human diseases. Studying the interaction between two loci is the natural progression
5 following the traditional and well-established single locus analysis. However, the added
6 costs and time duration required for the computation involved have thus far deterred
7 researchers from pursuing a genome-wide analysis of epistasis. In this paper, we propose a
8 method allowing such analysis to be conducted very rapidly. The method, dubbed
9 EPIBLASTER, is applicable to case-control studies and consists of a two-step process
10 where the difference in Pearson's correlation coefficients is computed between controls and
11 cases across all possible SNP pairs as an indication of significant interaction warranting
12 further analysis. For the subset of interactions deemed potentially significant, a second
13 stage analysis is performed using the likelihood ratio test from the logistic regression to
14 obtain the p-value for the estimated coefficients of the individual effects and the interaction
15 term. The algorithm is implemented using the parallel computational capability of
16 commercially available graphical processing units to greatly reduce the computation time
17 involved. In the current setup and example data-sets (211 cases, 211 controls, 299468
18 SNPs and 601 cases, 825 controls, 291095 SNPs), this coefficient evaluation stage can be
19 completed in roughly one day. Our method allows for exhaustive and rapid detection of
20 significant SNP pair interactions without imposing significant marginal effects of the single
21 loci involved in the pair.

22

1 **Introduction**

2 Understanding the effects of genes on phenotypes and diseases has long been suggested to
3 embed a complex form of interaction as a result of inter-inhibitory and -excitatory effects,
4 with any attempt to explain these effects simply as additive effects of the individual genes
5 being an overly simplistic model which ultimately provides an incorrect view of the genetic
6 influence on the phenotype.

7 The study of interaction between polymorphic loci can stem both from a biological and
8 statistical genetics perspective. The first approach establishes a model based on *a priori*
9 knowledge of how the genes function and interact. The latter, being a 'biological blind'
10 approach, helps draw inferences from previously unknown interdependencies between
11 genes. The ultimate objective, similar to all *black-box* studies, is to merge the conclusions
12 drawn from both approaches but since the observations made cannot be measured at a level
13 more finite than the eventual system output, the former approach is more likely to be
14 refined by first having a solid statistical finding as its basis.

15 As our effort primarily focuses on drawing statistical inference on epistatic
16 actions/interactions between genes, a new method is proposed to help improve our
17 capability to search and sift out significant interactions. This paper will discuss the
18 performance of our method in its current implementation. The results applied to a
19 simulated subset of SNPs and to two real genome-wide datasets recorded from panic
20 disorder and multiple sclerosis studies will be presented, followed by a discussion of some
21 properties of the approach.

22

1 **Materials and Methods**

2 **Overview of the two-stage search strategy**

3 The strategy consists of a two-stage approach. First, a filtering stage using the difference
4 of Pearson's correlation coefficients that performs an exhaustive two-locus interaction
5 multiplicative effects[1] search across all possible pairwise SNP combinations is
6 preformed. This is followed by logistic regression analysis on those subset of pairs deemed
7 significant in the previous stage.

8 **Data representation**

9 Each SNP is represented as integer values ranging from 0 to 2 based on the count of a
10 chosen reference nucleotide of the selected SNP for an allele dosage model, or as 0 or 1
11 depending on the genotype for a dominance or recessivity coding. In the current study, the
12 the allele dosage model is applied. An overall matrix is generated to store the information
13 of all SNPs as column vectors and the recorded values for individual subjects along the
14 rows. Column vectors are then analyzed in pairs and the correlation coefficients are
15 tabulated for cases and controls separately. Correlation coefficients are calculated from a
16 3×3 ordered genotype matrix, the genotypes being encoded 0,1,2. The difference between
17 the correlation coefficients in cases and controls is then computed and used as an indication
18 of the SNP pair contributing significantly to the classification between cases and controls
19 (please refer to Equation 1).

20 The first stage of analyzing the difference of correlations approach searches for
21 significant interaction terms. The second stage then computes the fit using a full rank
22 logistic model (Equation 2), including the intercept and additive marginal effects, on the

1 subset of loci pairing deemed significant from the first stage, from which a statistical test
2 can be conducted to test for the coefficient of interaction term being significantly different
3 from zero.

4 **Hardware and software setup**

5 The hardware used in the experimental setup consists of two pairs of commercially
6 available NVIDIA GTX295 GPUs running on a Intel Core i7 920 @ 2.67 GHz central
7 processing unit host (CPU) using 12 GB of DDR3 RAM. The software program is
8 implemented in R (version 2.9.2) with the 'gputools' package beta version 0.1-4 installed, in
9 which the function 'gpuCor' permits correlation coefficients to be tabulated for all possible
10 pairwise interactions across the column vectors using the CUDA (Compute Unified Device
11 Architecture) enabled NVIDIA graphic cards. The graphical card uses its parallel
12 computational capability to process independent evaluations faster than conventional CPU
13 based computation. Since the correlation coefficients between each SNP pair can be
14 tabulated independently, this can take full advantage of the inherent parallel computation
15 done on graphical cards. The overall time performance depends on the sample size and
16 desired marker coverage. A total evaluation of (number of SNPs choose 2) interactions is
17 typically accomplished within 24 hours for the entire data set (2000 individuals consisting
18 of 1000 cases, 1000 controls with 500000 SNPs) with the available GPU resources and the
19 given results retention criteria. Limitations on the speed can originate from local main
20 memory storage, memory transfer speed and number of on-board GPU cores present.
21 Some data partitioning to take advantage of all current GPU resource is thus required to
22 render this method most efficient. The dataset for the study is first partitioned into blocks

1 containing 2000 SNPs each that can be handled by the memory on the graphic card.

2 Hence, for a genome-wide dataset of 500k SNPs, 250 partitions are required.

3 The process goes through the entire dataset and calculates the correlation coefficients in
4 blocks of 2000 SNPs. The very first correlation analysis is performed is on the first
5 partition to itself, a 'partition-based autocorrelation', resulting in 1999000 unique
6 correlations. The process then increments the partition index of the second partition by one
7 and completes a correlation between two distinct sets of 2000 SNPs, a 'partition-based
8 cross-correlation', to yield 4 million unique results. This process of incrementing the
9 nested loop index is repeated until it reaches the last partition set at which point the top
10 level loop index gets incremented by one. The process can be summarized in the following
11 steps:

- 12 1. Partition the data set into size of 2000 SNPs. Note that this number may increase or
13 decrease depending on the number of individuals studied.
- 14 2. Set up a two-level nested loop to apply the partition-based correlation for all
15 possible SNP pairs for cases and controls separately.
- 16 3. Compute difference of correlation coefficients between cases and controls after
17 each partition-based autocorrelation or cross-correlation is complete.
- 18 4. Compute the p-values of each difference given that the distribution of the
19 differences follows a Gaussian.(refer to Results section).
- 20 5. Retain only SNP pairs that show a p-value below a selected threshold.
- 21 6. Repeat steps 3-5 across all partition pairs.
- 22 7. Proceed to stage 2 by performing a logistic regression on the selected pairs.

1 **Results**

2 **Simulated Data**

3 A simulated dataset is generated consisting of 2000 SNPs and a subject size of 5000
4 controls and 5000 cases. This simulated dataset is created without any specific model
5 allowing for any a priori knowledge of which particular pair will be significant, the purpose
6 is demonstrate the validity in the approximation of the resulting logistic regression
7 interaction term p-value to the approximation based on the difference in correlation
8 coefficients. The distribution of the differences of correlation coefficients is noted to
9 exhibit a Gaussian distribution within each partition set, referring to the histogram plot in
10 Figure1. This observation has been examined in greater detail by Gretton et al.[2] stating
11 that when samples are indeed drawn from two different distributions, the distribution of the
12 discrepancy of the chosen function, difference of estimated mean correlation coefficients
13 in this study, will converge to a Gaussian distribution. An additional proof for the
14 difference of correlation coefficients to exhibit a Gaussian distribution can be found in
15 Wellek and Ziegler[3], who have also shown that the variance of any single one difference
16 under the null hypothesis and thus also of the distribution of the sum of all differences is
17 the sum of the reciprocals of the number of cases and controls. For this Gaussianism it is
18 not needed that there are equal numbers of cases and controls.

19 In practice, to test for the significance of each pair, a Z-score is tabulated for each
20 difference within the partition set. This Z-score is computed based on the mean and the
21 standard deviation of all the differences noted within the partition set which is a close
22 approximation to the overall mean and standard deviation given that the partition size is

1 chosen to be large enough typically resulting in a few million pairs for each partition set.
2 Those interactions exhibiting a high overall Z-score are then taken as an indication that the
3 effect of the interaction term of the two SNPs in question is deemed valuable enough to be
4 passed on to the second stage. This filtered subset is then subjected to a second level of
5 mathematical-intensive evaluation using the likelihood ratio test on the logistic regression
6 model.

7 Referring to Figure 2, the p-values of the interaction product term in a general linear fit is
8 plotted against their correlation coefficient differences between cases and controls. To help
9 delineate any logarithmic trend, the p-values are shown as the negative logarithmic values.
10 As shown in Figure 2, there is a strong relationship between the two variables, of a
11 parabolic function in the region centered around the origin to a linear relationship in the
12 region of higher values. The region that is of most interest to the study is the higher
13 numerical value region as the p-values are the smallest and the differences are the largest.
14 Since the differences follow closely a Gaussian distribution (Figure 1), a Z-score threshold
15 can be used to estimate the retention rate. The statistic is then estimated using the fact that
16 the Z-score would follow a standard T-distribution with sufficiently large number of
17 degrees of freedom. A plot comparing the p-values obtained between the approximation
18 and the validation step is illustrated in Figure 3 and demonstrates a high R^2 value of 99.9%.
19 To help address the issues of limited physical disk space and of retaining only those
20 interactions that show strong significance, a Z-score of 4.5 was chosen as the cut-off
21 threshold, which corresponds to a probability of 6.8×10^{-6} retention rate. Thus, for the

1 partition-based autocorrelation generating ~ 2 million $\binom{2000}{2}$ correlation coefficient
2 differences, only the top 14 interaction pairs are expected to be retained. Overall, we
3 expect the top $\sim 8.5 \times 10^6$ pairs out of a possible $\sim 1.25 \times 10^{11}$ retained from the first
4 stage in a marker coverage of 500k SNPs.

5 **Real Data**

6 Real genetic data have been recruited from two separate published studies. The first
7 dataset originating from a panic disorder study [4] with a total of 299468 SNPs where 211
8 cases and 222 controls have been retained after standard quality control measures.
9 Computing the difference of correlation coefficients across all pairs and choosing a p-value
10 threshold of 1.0×10^{-5} resulted in a retention of 373153 SNP pairs. Similarly, a second
11 larger dataset from a multiple sclerosis [5] study with a total of 291095 SNPs in 601 cases
12 and 825 controls is also being investigated. Using the same p-value threshold of 1.0×10^{-5} ,
13 the 407660 most significant SNP pairs are retained upon subjecting it to the first stage.

14 In view of verifying that indeed no significant pairs have been left out in the adopted
15 difference of correlation coefficients stage of our method, a comparison to the p-values of
16 the interaction term in a normal linear regression of all possible SNPs pairs must be made.
17 To perform this brute-force approach in a time efficient manner, we have employed a
18 newly released software tool, FastEpistasis,[6] which is an extension to the PLINK
19 epistasis module capable of distributing the work in parallel on multiple CPU cores, it is
20 important to point out that this method is not working on the difference of Odds Ratio as
21 conducted by the Plink option bearing the same name. The program is meant to be
22 executed on quantitative phenotypes, but the difference in the p-values, which are the

1 relevant measure for this comparison, have been noted to be negligible on several sample
2 SNP pairs (see also Table 1, comparing the FastEpistasis column to the logistic regression
3 interaction term p-value column, but also simulation studies (refer to Supplementary Figure
4 1)). The p-values computed from FastEpistasis is regarded to be the “true” value used for
5 comparison to the approximated method described in stage 1 of EPIBLASTER.

6 Matching the results from SNP pairs with p-values below 1×10^{-6} tested against null from
7 the FastEpistasis with the results obtained from the first stage of EPIBLASTER is
8 performed. From the panic disorder analysis, FastEpistasis produced 37336 SNP pairs of
9 which 36056 of them are also found in the EPIBLASTER stage 1 retained subset (96,5%).
10 The unmatched pairs are indeed examples where EPIBLASTER stage 1 underestimates the
11 p-values and the hard threshold prevents it from being included, thus, these unmatched
12 pairs all are in fact situated around the p-values threshold region and are of lesser
13 significance compared to the others. The plot of the matching pairs are shown on Figure 4
14 and for ease of visualization, it is illustrated as a smoothed color density of the actual
15 scattered points plot. The top 10 most significant pairs from the FatEpistasis approach are
16 listed with greater details in Table 1 along with their annotations in Table 2 and are marked
17 with a dark circle on Figure 4. In order for EPIBLASTER stage 1 to capture all top 10
18 pairs of the “true” approach (FastEpistasis), a p-value threshold of 1.26×10^{-8} must be
19 applied, thus resulting in the top 387 pairs of EPIBLASTER stage 1 to be passed onto stage
20 2. In other words, EPIBLASTER would have produced an additional 377 pairs to be tested
21 in view of capturing the very top 10 true results. In Figure 5, the top 100 SNP pairs of the
22 panic disorder study are marked, which would have resulted in applying a retention

1 threshold for EPIBLASTER stage 1 of 1.67×10^{-7} passing on some 5194 pairs to stage 2.
2 From the multiple sclerosis analysis, FastEpistasis yielded 42731 pairs to have an
3 interaction term with a p-value below 1×10^{-6} of which 42524 pairs (99.5%) are also
4 retained from EPIBLASTER stage 1. The matching pairs along with the respective p-
5 values tabulated using the FastEpistasis method versus the approximated EPIBLASTER
6 stage 1 method are plotted in Figure 6. The top ten pairs are marked in Figure 6 and listed
7 in Table 3 along with the SNP annotations in Table 4. In order for EPIBLASTER to
8 capture the top 10 pairs, it would have required a 48 of its top significant SNP pairs to be
9 carried over to stage 2 where the p-values from logistic regression are tabulated. In
10 addition, in order to capture the top 100 pairs (listed in greater details in Supplementary
11 Table 2), EPIBLASTER would have required the top 19242 pairs obtained from stage 1 to
12 be passed on to stage 2.

13 **Discussion**

14 Although the search is conducted across all possible pairwise SNP interactions, the main
15 interest is to delineate interactions between unlinked loci that influence the illness. In the
16 first stage, the difference of Pearson's correlation coefficients, tabulated from the SNP pair,
17 is taken between controls and cases across all possible interactions. In addition, this step
18 can also incorporate replicating for significant association across two or more independent
19 studies using a number of subjects weighted meta-analysis during the actual run. In the
20 current experimental setup with a genome-wide analysis of epistasis study, this first stage
21 involving the difference of correlation coefficient evaluations can be completed within
22 roughly 24 hours on commercially available GPU set-up compared to roughly a year on a

1 single-core CPU. From the subset of interactions deemed significant in the rapid filtering
2 stage, a second stage analysis is performed using the likelihood ratio statistical test on the
3 logistic regression to obtain the p-value on the estimated coefficients corresponding to the
4 intercept, individual effects of the single loci and the interaction terms. As this necessitates
5 only a minor amount of computations of logistic regressions in R using 'anova' test on the
6 'glm' fit with the 'binary' family option, for a retention rate of 6.8×10^{-6} , an expected
7 8.5×10^6 pairs, this requires some 2.5 days on a single core system of the hardware
8 specifications listed in the methods section in R. This is impractical, however, if we are to
9 limit ourselves to a range of top significant pairs which can be below a more stringent
10 threshold, e.g. 1.0×10^{-8} , it drops down to an expected number of some 600-700 pairs,
11 which requires around 150 seconds (4 computations per second) to validate. It should be
12 noted that dedicated software, such as INTERSNP [7] is considerably faster for this second
13 pass than pure R, the quoted figure of 8.5×10^6 interaction pairs should be done between
14 one or two hours using INTERSNP. A complete genome-wide association analysis with
15 INTERSNP on a single core would be in the order of a year. FASTEPISTASIS would
16 have been some 70 days on a single core. Note that INTERSNP is quoted here for a full
17 logistic regression, whilst FASTEPISTASIS does a linear regression. Of course the
18 performance of both INTERSNP (which again is about two orders of magnitude faster than
19 plain R [using the glm() function]) and FASTEPISTASIS can be easily improved using
20 multi-core systems and clusters.

21 Including more SNPs into the second stage is feasible, of course. We have found a
22 threshold of 6.8×10^{-6} practical, lowering this by e.g. one order of magnitude will incur only

1 a slight increase in run-time for stage 1 and a linear increase for stage 2. Of course, if the
2 threshold for entry into stage 2 is lowered too much, hardware specifics such as disk speed
3 is becoming an issue in the performance of the program.

4 The reasoning behind the two-stage approach is threefold. First, the computations involved
5 in the first stage are much less extensive as compared to estimating for significance in
6 logistic regression. Second, a readily available R package, 'gputools', allows the estimation
7 of correlation coefficients to be performed on the graphic card which greatly reduces the
8 time and cost. Third, contrary to common multistage practice where the single locus test is
9 performed initially followed by higher order testing on loci which showed single locus
10 significance, the necessity of interaction loci to first show significant marginal effects is not
11 imposed, thus rendering this method a truly exhaustive search across all two-way
12 interactions. The results from the MS and Panic disorder analyses are used as preliminary
13 basis where this statement can be founded. A Plink method to test for univariate SNP
14 significance is used to provide an indication of the SNPs that would be kept using the more
15 traditional mandatory main effect significance. Firstly, referring to Tables S.2 and S.3 in
16 the supplemental section, it is shown that a vast majority of significant interaction pairs
17 would not have been captured if one is to pre-filter based on univariate significance.

18 Furthermore, referring to Figures S.2 to S.5 in the supplemental section, univariate p-values
19 are plotted against the interaction pairs captured by EPIBLASTER, the lack of trends helps
20 support that the method is indeed conducting the search unbiased to the marginal effects at
21 the two loci. High overestimation of the significance of the pair in the preliminary step
22 one filtering stage can occur when the SNPs are very rare. Severe underestimating of the

1 p-values using this approximation (false negatives) has also rarely been noticed but was
2 traced to a small subset of those SNP pairs that are in high linkage disequilibrium, which
3 are not the main focus of this method. For computational ease, no lower bound on physical
4 distance between SNPs or on LD between SNPs is imposed.

5 We also noted no inflation of the test statistic in our datasets, however, in cases it might be
6 advisable to include MDS or PCA components in the analysis, e.g. by working on
7 residuals of the SNP genotypes on these components.

8

9 Overall, comparing the p-values obtained from FastEpistasis to the approximated p-
10 values tabulated from EPIBLASTER stage 1 show that although discrepancy in the p-
11 values do exist, the adopted method does manage to capture all of the significant pairs and
12 the occurrence of significant pairs being omitted is practically nil when the threshold p-
13 values is chosen to be far enough from the Bonferroni corrected global significance. Still
14 the computational load for the second stage analysis is negligible.

15 The concept of adopting the analysis of the difference of case-only and control-only
16 studies into an unified test has been suggested in prior studies analyze pairwise SNPs. Hoh
17 and Ott [8] initially proposed taking the ratios of the Chi-squares of the 3x3 contingency
18 tables between cases and controls as a measure of significance. Zhao et al.[9] and Zaykin
19 et al[10] have also proposed examining the gene interactions with a defined Linkage
20 Disequilibrium created by the interaction between two unlinked loci. Significance is
21 evaluated with the analysis of the difference of the LD values between case-only and
22 control-only populations. Hardy-Weinberg Equilibrium must hold for this measure of

1 interaction and test statistics to be valid. Zhao et al. has further suggested the method
2 exhibits greater power than conventional linear regression, as it does not treat the
3 interaction as a residual term and allows for implicit nonlinear interaction, and faster
4 computational time than the traditional four degrees of freedom logistic regression model
5 rendering it more suitable for GWAS. The proposed method in this paper performs the
6 search in the first stage for only the effects of the interaction term by analyzing the
7 difference of the correlation coefficients as an indication for significance and then adopts
8 the more conventional logistic regression method to substantiate the findings on a subset of
9 pairs. As the difference is based on two separate groups, population stratification can have
10 an effect on the power of the method. However, looking at the number of pairs retained
11 from our examples, the actual inflation is very low. In the multiple sclerosis analysis,
12 423680 pairs is expected be below the 1×10^{-5} threshold, an observed number of pairs
13 captured is noted as 407660. The method can indeed be simplified to a case-only study, by
14 making the assumption that the correlation coefficient of the controls be null for all pairs,
15 this approach would further speed up the computational time by a factor of 2 at the expense
16 of potentially losing both potentially power and clearly precision. Moreover, the
17 approximation approach does not only apply to the dosage coding (0, 1, 2), but also to
18 other coding such as dominance, recessivity and heterozygosity. In general a p-value
19 cutoff of less than 1×10^{-5} should indeed be sufficient to capture all the results with a p
20 $< 1 \times 10^{-8}$ in the logistic regression and is, with all caution, suggested as a cut-off to be used
21 in a first analysis, truly making EPIBLASTER exhaustive within this setting.
22 With respect to the results from MS and panic disorder presented we note that, although,

1 there is no pair beyond a Bonferroni corrected threshold for significance at a corrected p-
2 value of 0.05, the marginal effects in the top 10 pairs do not at all show a tendency to
3 deviate from a uniform distribution. This means that prefiltering pairs of SNPs on marginal
4 p-values for subsequent epistasis analysis may be a less promising strategy than sometimes
5 considered, although more analyses and larger sample sizes will be needed for a better
6 founded statement on this issue.

7 In the editing phase of this article, it has come to our attention that Hu et al.[11] have also
8 developed a strategy involving GPUs to enhance genome-wide significant SNP pair
9 interaction search, quoting a total runtime of 27 hours to scan through the Wellcome Trust
10 Case Control Consortium's bipolar disorder data consisting of 500k SNPs. The proposed
11 algorithm by Hu et al. helps consolidate the improved time performance using the inherent
12 parallel nature of GPU to search for significance in all possible SNP pairs. The method is
13 distinct from ours as it uses the a difference of odds ratios measure between cases and
14 controls to pick significant SNP pair candidates.

15 We would like to point out that with EPIBLASTER it is possible to perform genome-
16 wide analysis of epistasis on very small-scale and inexpensive hardware, reducing the need
17 for large clusters for this kind of application.

18 Future work is planned to incorporate the logistic regression and other more novel
19 definitions of gene-gene interactions onto the graphical processing units. EPIBLASTER is
20 available at <http://www.mpipsykl.mpg.de/epiblaster>.

21

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8 **Conflict of Interest Statement**

9 The authors declare no conflict of interest.

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12 **Supplementary information is available at European Journal of Human Genetics'**
13 **website**

14

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Figures, Equations and Tables.

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1 Equations

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3 Equation 1. Correlation coefficients (Pearson) difference between case-only and control-
4 only for each SNP-SNP pair. Note that no assumptions, such as HWE to hold, are needed
5 here.

6

7

$$\text{Difference of Correlation Coefficients} = \Delta =$$

8

9

$$\sum_{i \in \text{cases}} \left\{ \frac{(\text{SNP1}_i - \overline{\text{SNP1}_i})(\text{SNP2}_i - \overline{\text{SNP2}_i})}{(n_i - 1)\sigma_{\text{SNP1}_i}\sigma_{\text{SNP2}_i}} \right\} - \sum_{j \in \text{controls}} \left\{ \frac{(\text{SNP1}_j - \overline{\text{SNP1}_j})(\text{SNP2}_j - \overline{\text{SNP2}_j})}{(n_j - 1)\sigma_{\text{SNP1}_j}\sigma_{\text{SNP2}_j}} \right\}$$

10 The variance of each one of these correlation coefficients is, as shown by Wellek and

11 Ziegler [3], equal to $\frac{1}{n-1}$ where n is the respective number of cases and controls. As the

12 cases and controls constitute, obviously, independent samples, the total variance V_{tot} is then
13 the sum of the two single variances. As a consequence and from both Gretton et al[2] and

14 Wellek and Ziegler[3] thus $T = \Delta / V_{\text{tot}}^{1/2} \sim N(0,1)$.

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19 Equation 2. Full rank logistic regression model.

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$$\text{Phenotype} = \text{Intercept} + \alpha\text{SNP1} + \beta\text{SNP2} + \gamma\text{SNP1*SNP2}$$

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Titles and legends to figures.

Figure 1. Histogram of differences of correlation coefficients of all 2-way interactions of 2000 SNPs exhibiting the expected Gaussian distribution shape.

Figure 2. Logarithmic p-values from interaction term of logistic regression versus correlation coefficient differences of all 2-way interactions from 2000 SNPs.

Figure 3. Logarithmic p-values from interaction term of the logistic regression model versus correlation coefficient differences p-values from 2000 SNPs (2000C2 = 1999000 SNP-SNP pairs). Quality of Fit (R²) between the p-values is 99.9%.

Figure 4. Panic disorder logarithmic p-values density plot: Top 10 SNP pairs (points marked in black) and threshold correlation coefficient difference p-value. FastEpistasis p-values are on the y-axis, p-values from EPIBLASTER on the x-axis.

Figure 5. Panic disorder logarithmic p-values density plot: Top 100 SNP pairs (points marked in black) and threshold correlation coefficient difference p-value. FastEpistasis p-values are on the y-axis, p-values from EPIBLASTER on the x-axis.

Figure 6. Multiple sclerosis logarithmic p-values density plot: Top 10 SNP pairs (points marked in black) and threshold correlation coefficient difference p-value

Figure 7. Multiple sclerosis logarithmic p-values density plot: Top 100 SNP pairs (points marked in black) and threshold correlation coefficient difference p-value.

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Table 1. Top 10 panic disorder SNP pairs difference of correlation coefficient, FastEpistasis and logistic regression p-values.

Top 10 Panic Disorder SNP pairs ranked by FastEpistasis									
Ranking	SNP1 Name	SNP2 Name	Diff. of R	Diff. Of R Pvalue	FastEpistatic Pvalue	ureg-SNP1 Pvalue	ureg-SNP2 Pvalue	ureg-Interaction Pvalue	
1	rs4653309	rs17338700	0,61	2,26E-10	6,97E-12	1,94E-01	6,16E-01	8,98E-12	
2	rs4984422	rs1967113	-0,66	8,86E-12	1,06E-11	2,02E-01	8,66E-01	4,72E-13	
3	rs1156847	rs7246846	0,62	1,21E-10	6,57E-11	7,45E-01	2,01E-01	4,02E-11	
4	rs6455842	rs265548	0,64	2,81E-11	7,25E-11	3,67E-01	3,55E-01	6,17E-12	
5	rs12188192	rs1317584	0,58	1,98E-09	8,08E-11	2,51E-01	4,90E-01	1,87E-10	
6	rs2100807	rs4875302	0,61	1,95E-10	1,88E-10	7,15E-01	3,95E-01	1,45E-10	
7	rs11900448	rs11939830	-0,6	5,07E-10	2,17E-10	2,27E-01	7,97E-01	2,64E-10	
8	rs6762261	rs4745430	0,61	3,24E-10	2,36E-10	4,81E-01	1,87E-01	1,65E-10	
9	rs2374344	rs1011308	0,55	1,26E-08	2,53E-10	3,97E-01	4,00E-01	4,41E-10	
10	rs11925795	rs4731772	0,62	1,60E-10	3,11E-10	3,49E-03	4,37E-01	4,71E-10	

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Table 2. Top panic disorder SNP pairs annotations.

Top10 Panic Disorder SNP pairs ranked by FastEpistasis Annotations							
SNP1 Name	Chromosome	Basepair	Gene	SNP 2 Name	Chromosome	Basepair	Gene
rs4653309	chr1	37876927		rs17338700	chr2	33841677	
rs4984422	chr15	94456392		rs1967113	chr18	26830011	DSC3
rs1156847	chr9	2586783		rs7246846	chr19	56705171	
rs6455842	chr6	162962566	PARK2	rs265548	chr19	17763334	
rs12188192	chr5	136380739	SPOCK1	rs1317584	chr6	12450775	
rs2100807	chr3	117506680	LSAMP	rs4875302	chr8	4028885	CSMD1
rs11900448	chr2	149650765	LOC130576	rs11939830	chr4	157150631	
rs6762261	chr3	136073828	EPHB1	rs4745430	chr9	77461845	
rs2374344	chr2	41994977		rs1011308	chr9	72478076	
rs11925795	chr3	178001610		rs4731772	chr7	130582931	

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Table 3. Top 10 multiple sclerosis SNP pairs difference of correlation coefficient, FastEpistasis and logistic regression p-values.

Top 10 multiple sclerosis SNP pairs ranked by FastEpistasis								
Ranking	SNP1 Name	SNP2 Name	Diff. of R	Diff. Of R Pvalue	FastEpistatic Pvalue	ureg-SNP1 Pvalue	ureg-SNP2 Pvalue	ureg-Interaction Pvalue
1	rs1392773	rs1384731	0,36	3,68E-11	3,78E-12	7,00E-01	9,90E-01	4,28E-12
2	rs1552621	rs6817936	0,34	2,00E-10	5,87E-11	7,85E-01	6,75E-01	6,71E-11
3	rs11710441	rs13226149	-0,33	5,92E-10	7,28E-11	4,79E-01	2,21E-01	8,66E-11
4	rs2218314	rs1384731	0,33	8,68E-10	8,19E-11	6,11E-01	9,99E-01	9,34E-11
5	rs6738313	rs3752735	-0,34	3,18E-10	1,03E-10	1,91E-01	7,18E-01	1,12E-10
6	rs7593466	rs11658318	0,34	3,14E-10	1,07E-10	7,66E-01	1,83E-01	1,01E-10
7	rs6758449	rs10055397	0,34	3,64E-10	1,09E-10	3,23E-01	6,90E-01	1,16E-10
8	rs17648731	rs7386137	0,35	1,22E-10	1,10E-10	8,15E-01	6,03E-01	1,05E-10
9	rs6550306	rs10503253	0,34	4,17E-10	1,52E-10	9,32E-01	3,58E-01	1,66E-10
10	rs2542509	rs2916433	0,34	5,04E-10	1,71E-10	6,94E-02	9,53E-01	1,81E-10

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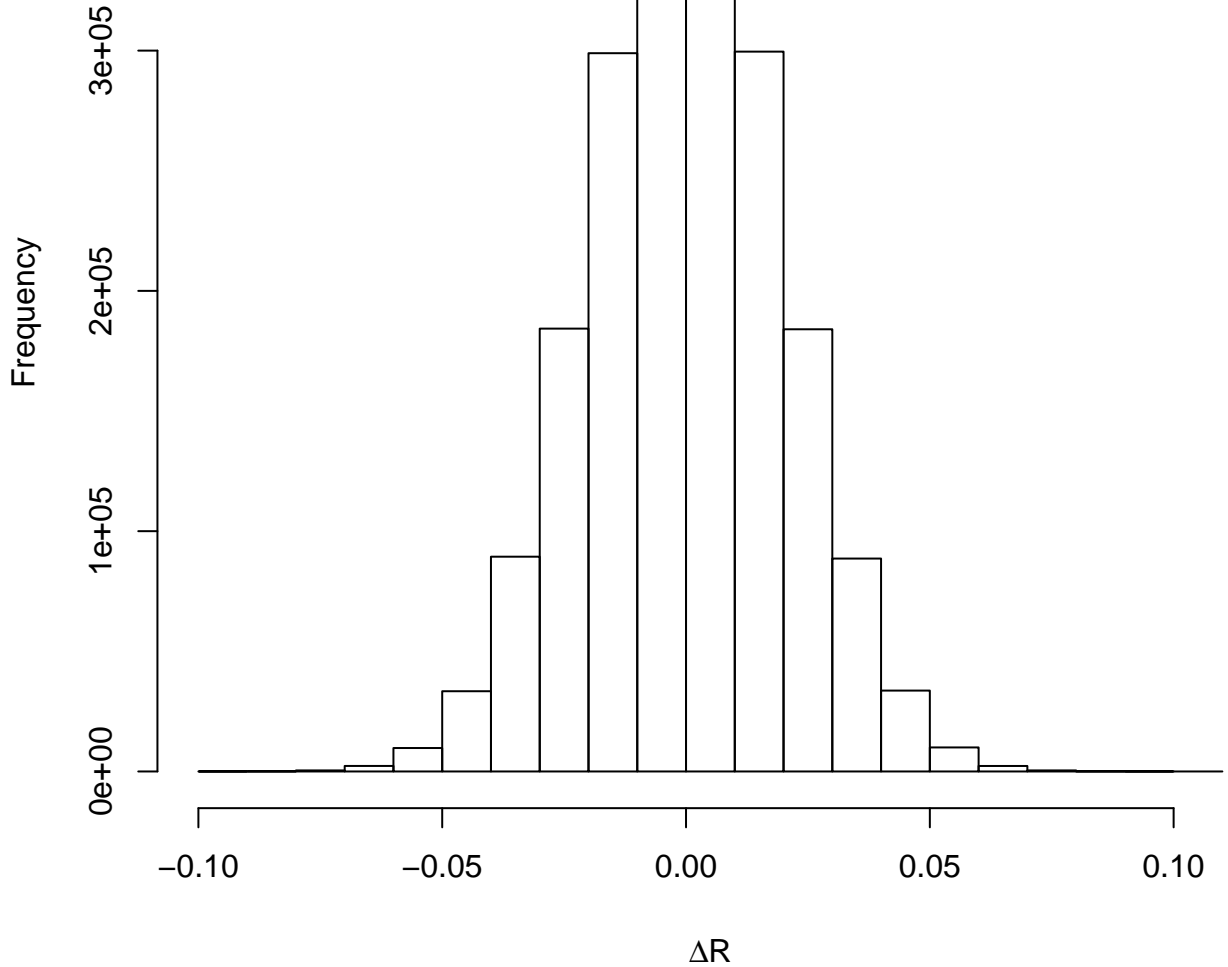
Table 4. Top 10 multiple sclerosis SNP pairs annotations.

Top10 Multiple Sclerosis SNP pairs ranked by FastEpistasis Annotations							
SNP1 Name	Chromosome	Basepair	Gene	SNP 2 Name	Chromosome	Basepair	Gene
rs1392773	chr4	143053312		rs1384731	chr5	10660797	
rs1552621	chr3	67460533		rs6817936	chr4	167934823	SPOCK3
rs11710441	chr3	145154009		rs13226149	chr7	94863536	PON3
rs2218314	chr4	143031581		rs1384731	chr5	10660797	
rs6738313	chr2	3382368	TTC15	rs3752735	chr18	49363018	
rs7593466	chr2	208807724	IDH1	rs11658318	chr17	27230172	UTP6
rs6758449	chr2	68290612	PPP3R1	rs10055397	chr5	120950796	
rs17648731	chr2	77575007		rs7386137	chr8	142596655	
rs6550306	chr3	34873129		rs10503253	chr8	4168252	CSMD1
rs2542509	chr2	71443251	ZNF638	rs2916433	chr4	4343724	LYAR/ZNF509

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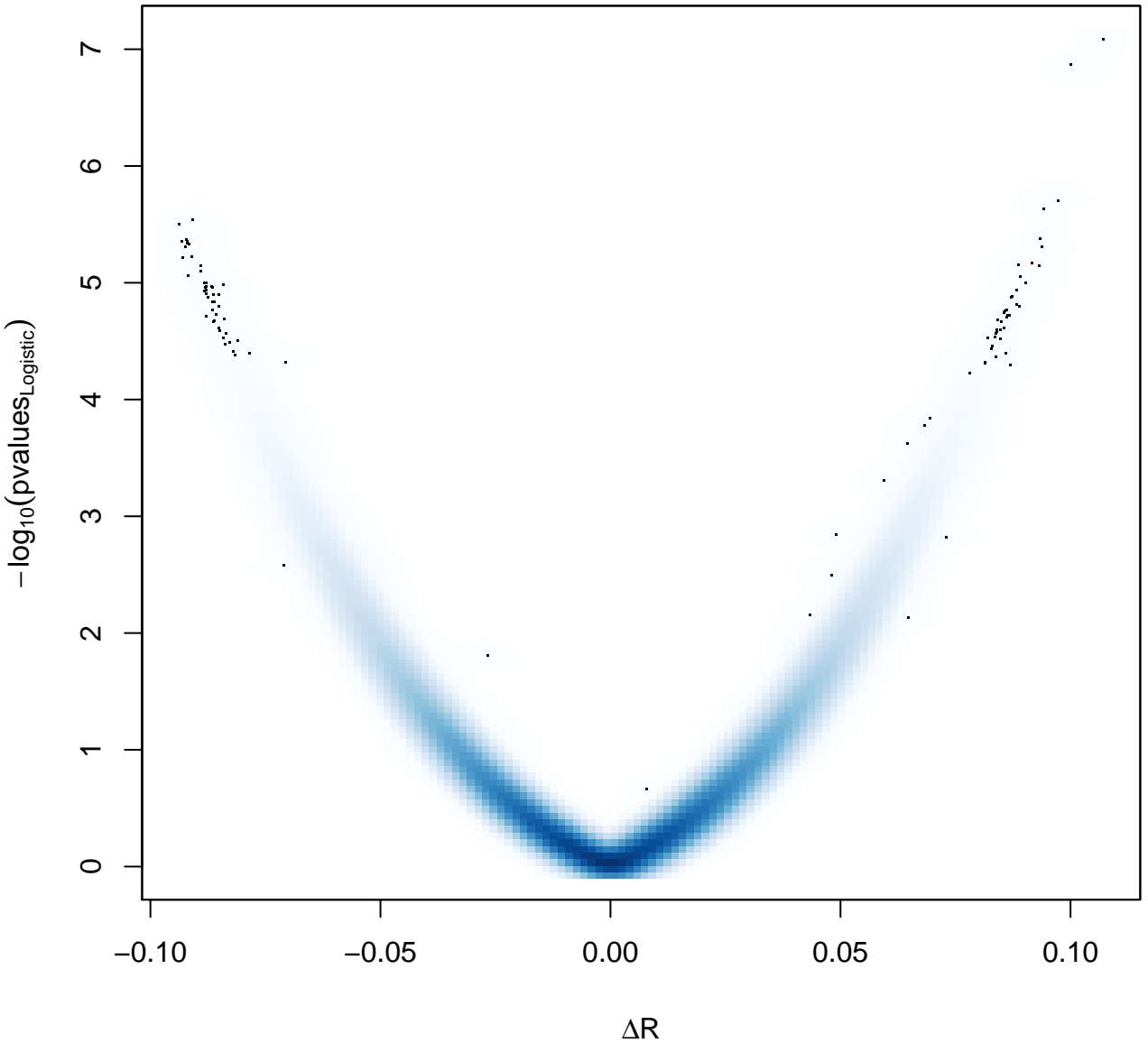
Simulation Data

Distribution of Correlation Coefficients Difference



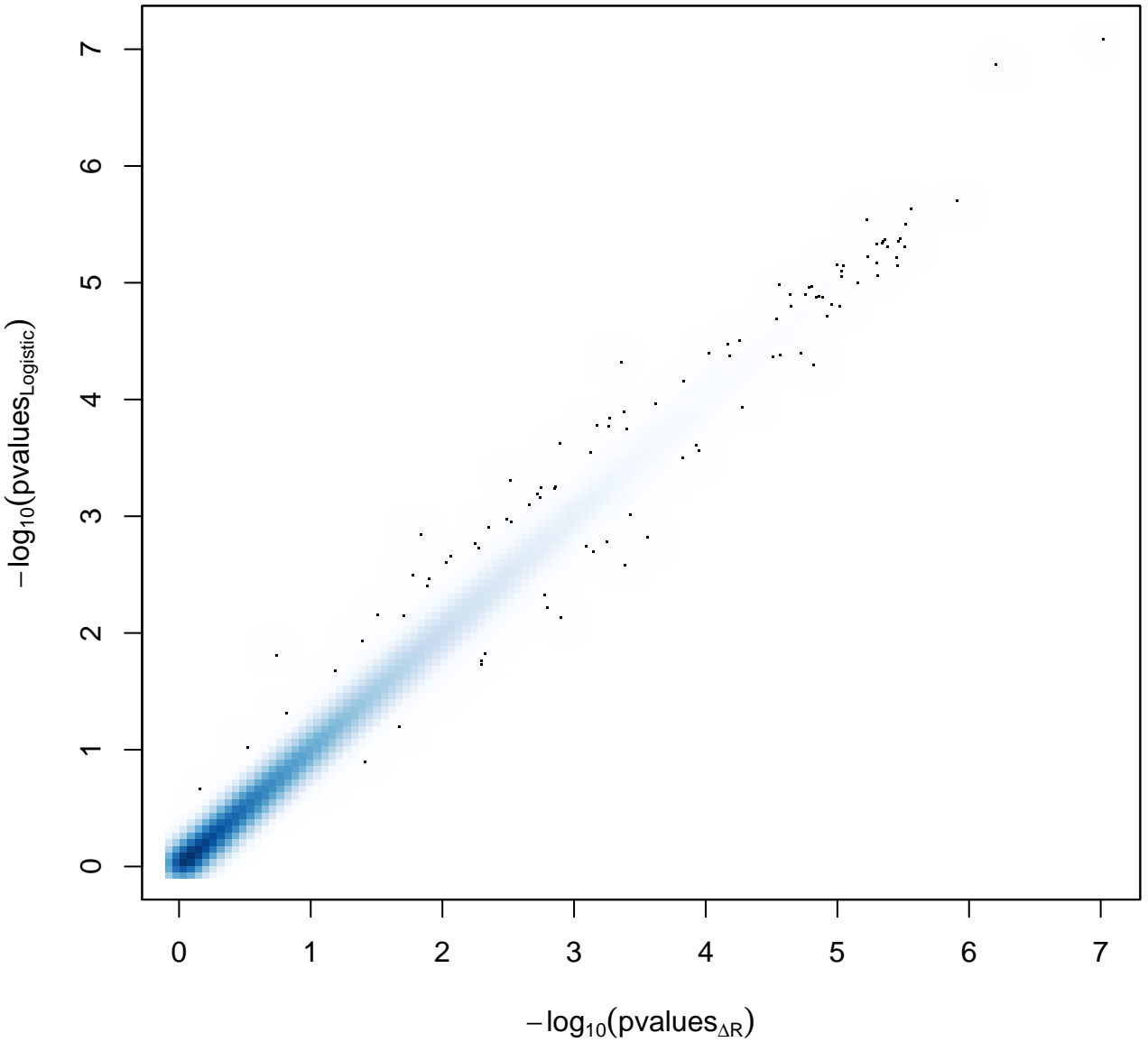
Simulation Data

Logistic Regression p-values vs. Correlation Coefficients Difference



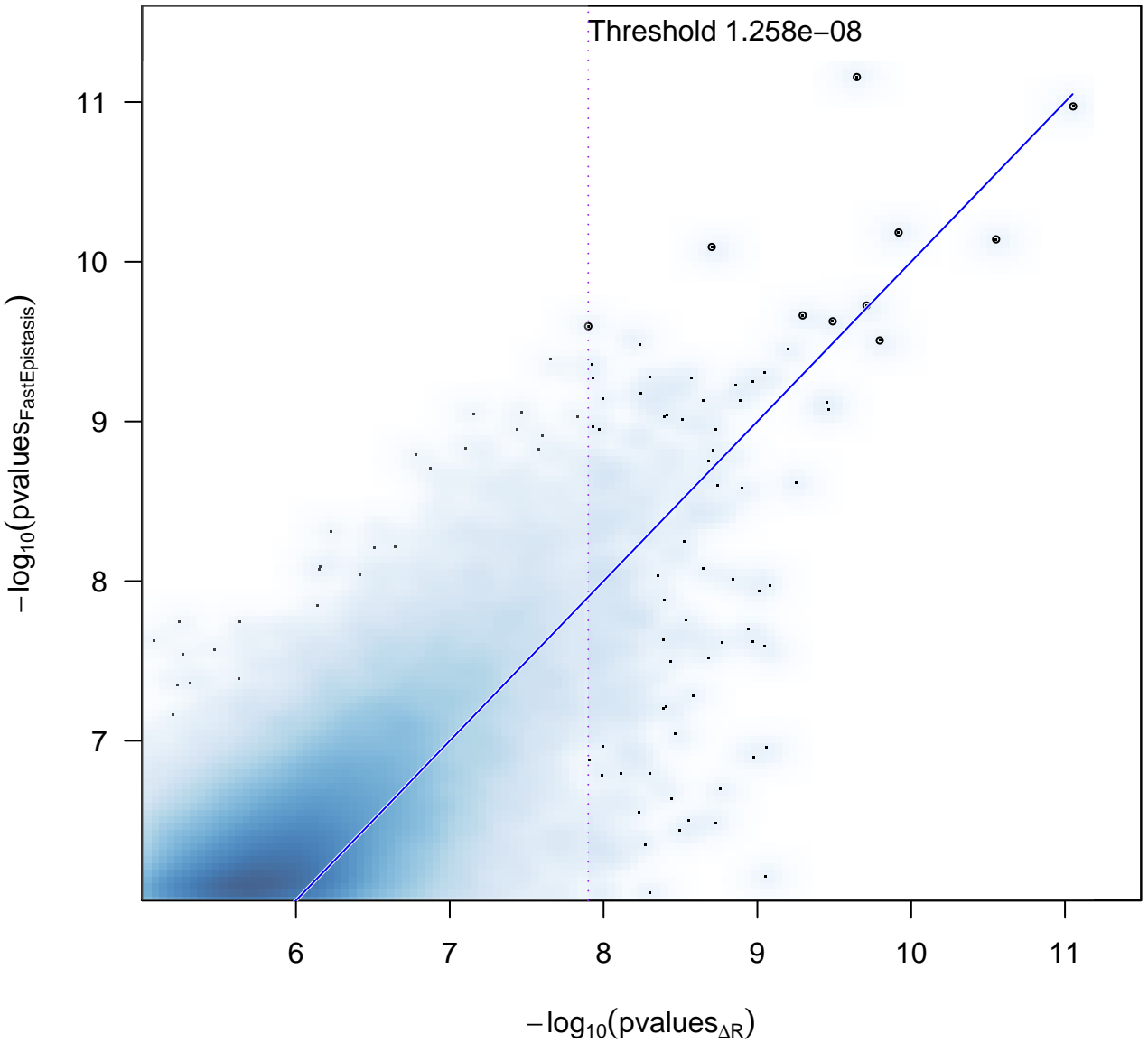
Simulation Data

Logistic Regression p-values vs. Correlation Coefficients Difference p-values



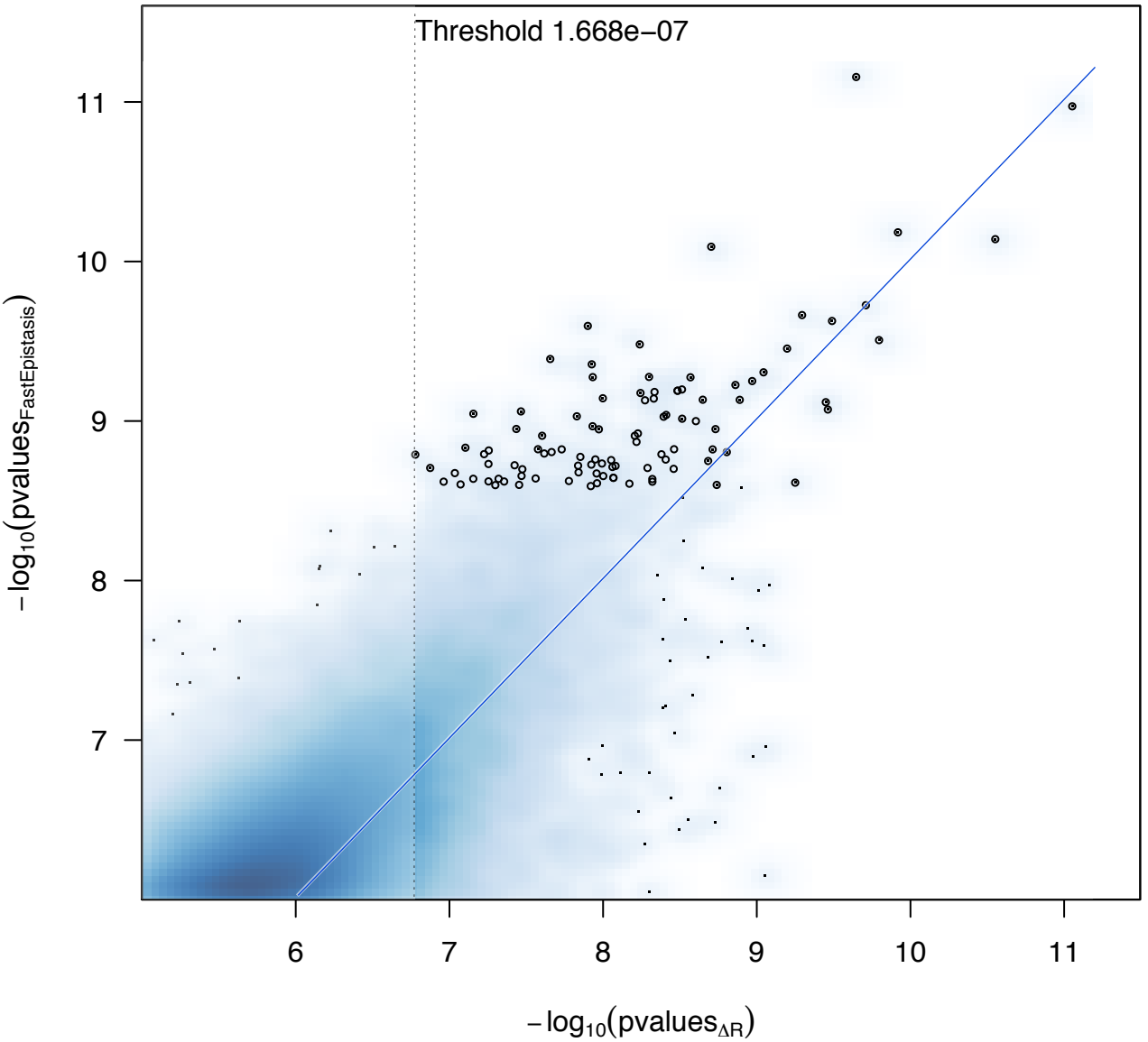
Panic disorder

FastEpistasis versus correlation coefficient difference pvalues



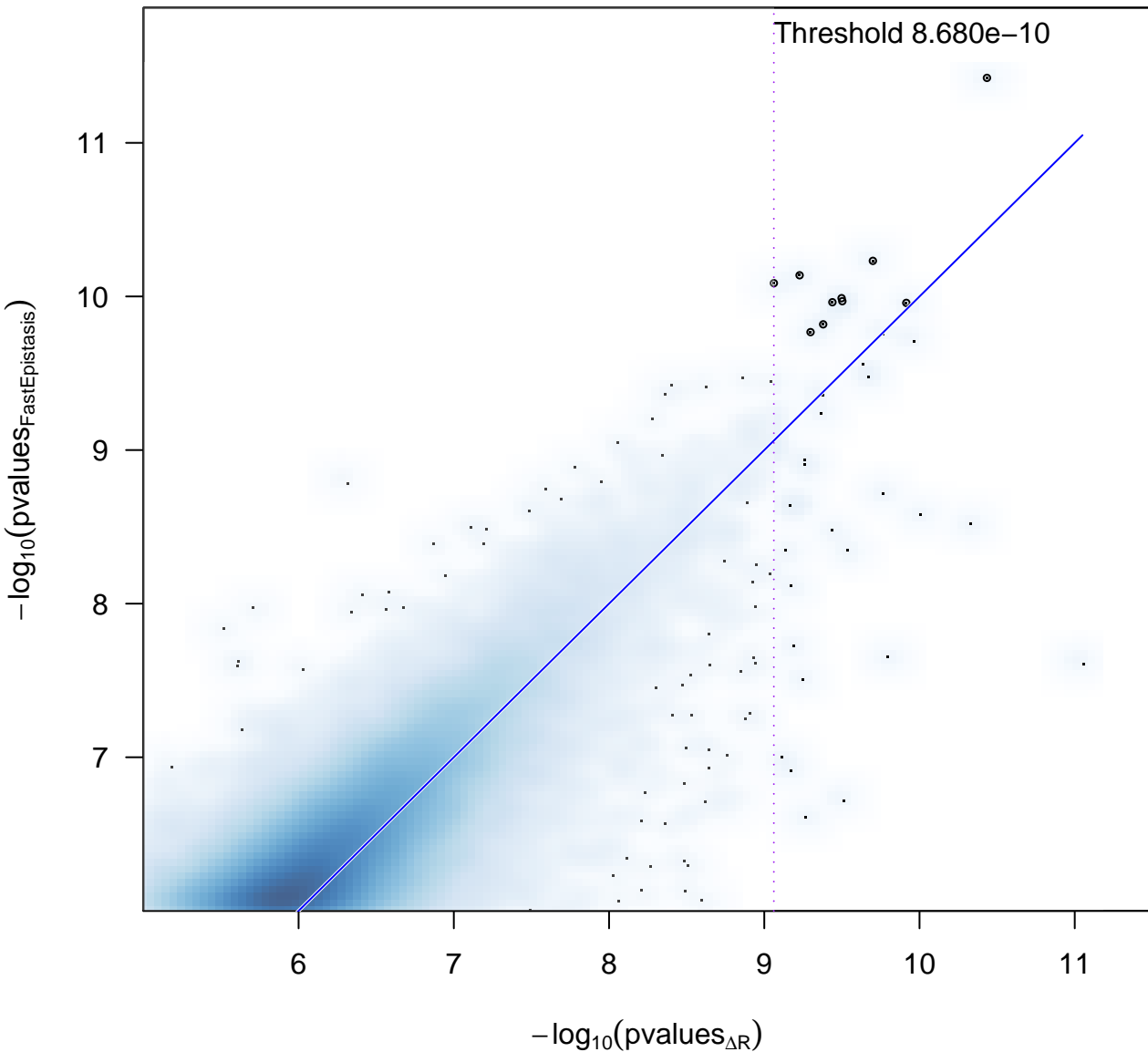
Panic disorder

FastEpistasis versus correlation coefficient difference pvalues



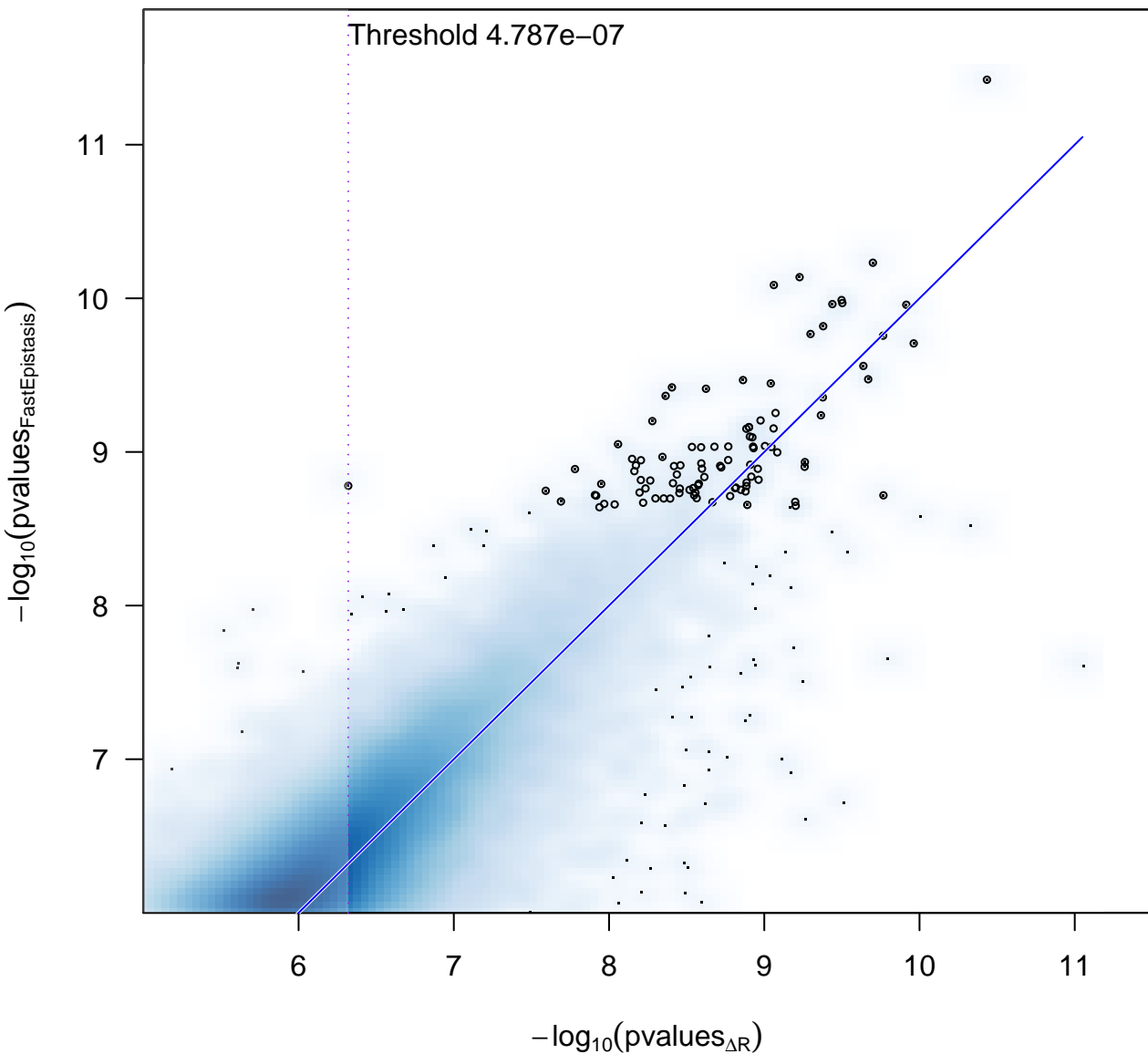
Multiple Sclerosis

FastEpistasis versus correlation coefficient difference pvalues



Multiple Sclerosis

FastEpistasis versus correlation coefficient difference pvalues



Supplemental Material

Supplemental figures

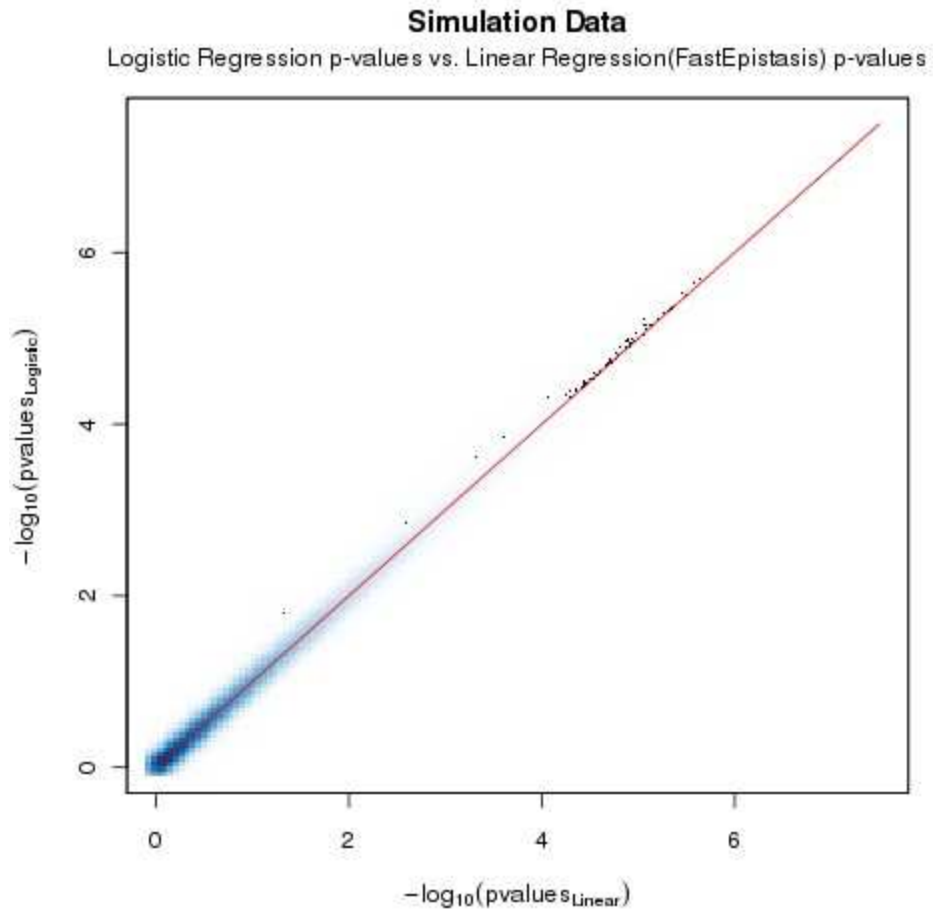


Figure.S 1. Logarithmic p-values from interaction term of the logistic regression model versus linear regression model. ($R^2=99.9\%$). Red line marks unit slope line.

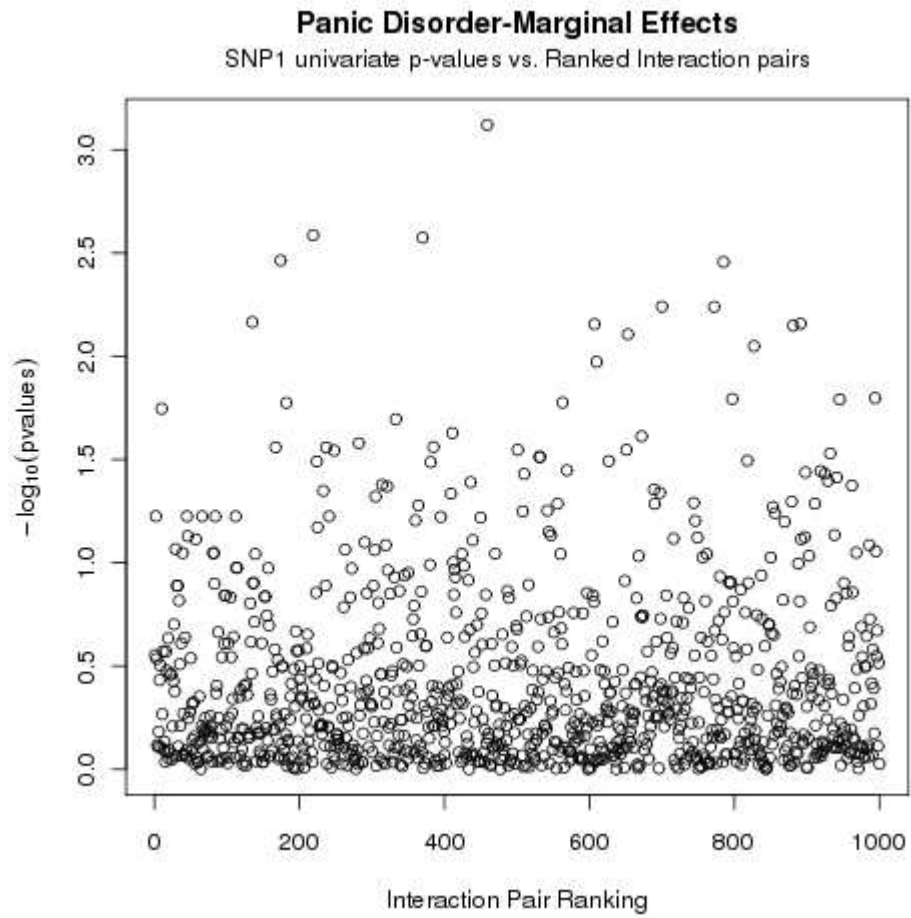


Figure.S 2: Panic Disorder SNP1 univariate P-values versus EPIBLASTER interaction pair ranking for top 1000 pairs.

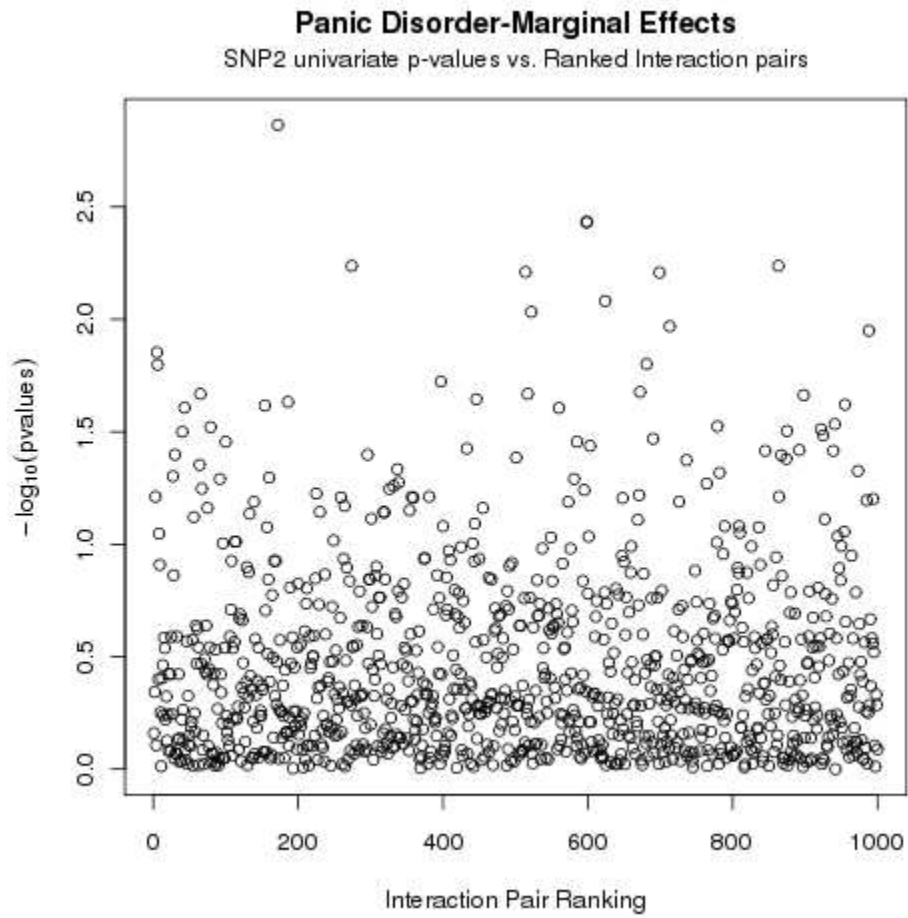


Figure.S 3: Panic Disorder SNP2 univariate P-values versus EPIBLASTER interaction pair ranking for top 1000 pairs.

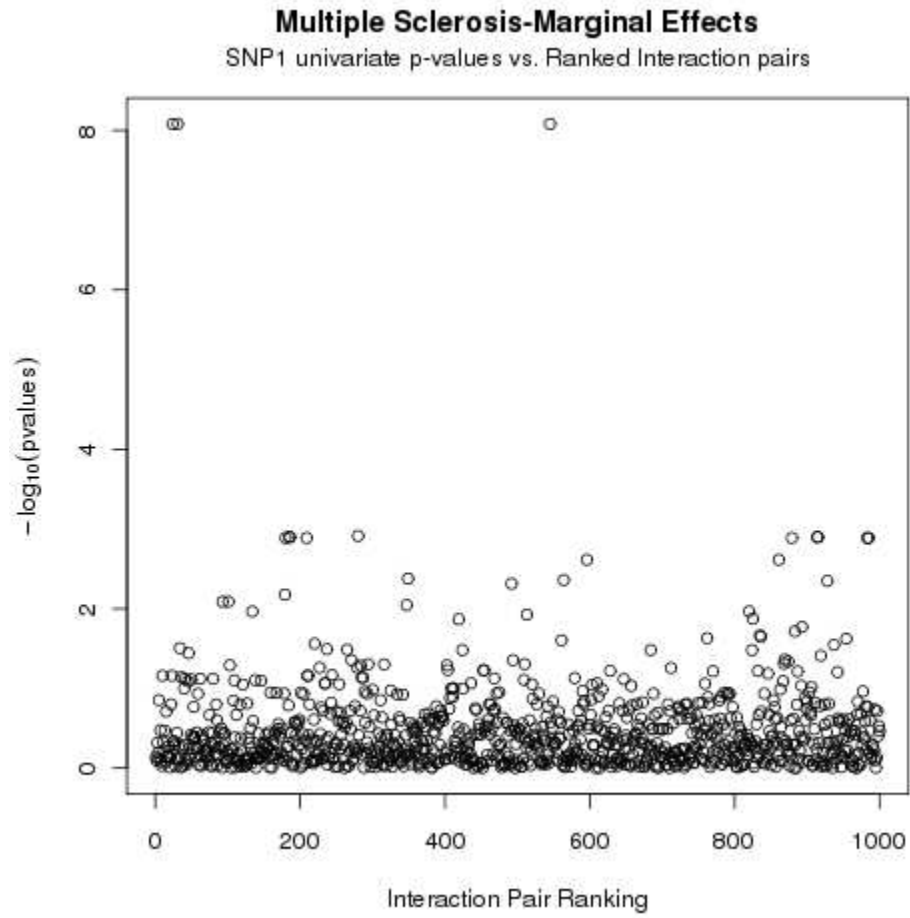


Figure.S 4: Multiple Sclerosis SNP1 univariate P-values versus EPIBLASTER interaction pair ranking for top 1000 pairs.

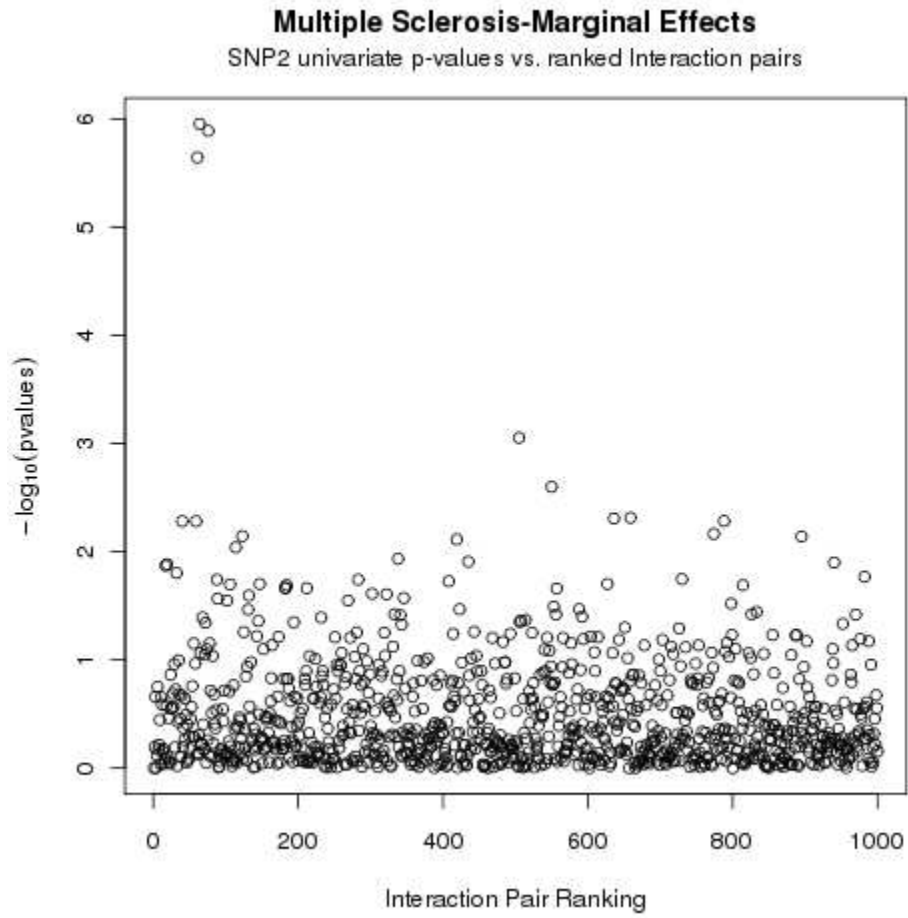


Figure.S 5: Multiple Sclerosis SNP2 univariate P-values versus EPIBLASTER interaction pair ranking for top 1000 pairs.

Supplemental tables

Table S.1 Top 100 Panic disorder SNP pairs ranked by FastEpistasis

Rank	SNP1 Name	SNP2 Name	Diff. of R	Diff. Of R Pvalue	FastEpistatic Pvalue	Lreg-SNP1 Pvalue	Lreg-SNP2 Pvalue	Lreg-Interact Pvalue
1	rs4653309	rs17338700	0.61	2.26E-010	6.97E-012	1.94E-001	6.16E-001	8.98E-012
2	rs4984422	rs1967113	-0.66	8.86E-012	1.06E-011	2.02E-001	8.66E-001	4.72E-013
3	rs1156847	rs7246846	0.62	1.21E-010	6.57E-011	7.45E-001	2.01E-001	4.02E-011
4	rs6455842	rs265548	0.64	2.81E-011	7.25E-011	3.67E-001	3.55E-001	6.17E-012
5	rs12188192	rs1317584	0.58	1.98E-009	8.08E-011	2.51E-001	4.90E-001	1.87E-010
6	rs2100807	rs4875302	0.61	1.95E-010	1.88E-010	7.15E-001	3.95E-001	1.45E-010
7	rs11900448	rs11939830	-0.6	5.07E-010	2.17E-010	2.27E-001	7.97E-001	2.64E-010
8	rs6762261	rs4745430	0.61	3.24E-010	2.36E-010	4.81E-001	1.87E-001	1.65E-010
9	rs2374344	rs1011308	0.55	1.26E-008	2.53E-010	3.97E-001	4.00E-001	4.41E-010
10	rs11925795	rs4731772	0.62	1.60E-010	3.11E-010	3.49E-003	4.37E-001	4.71E-010
11	rs1001763	rs1584407	0.56	5.77E-009	3.31E-010	4.32E-001	2.92E-001	1.86E-010
12	rs7776948	rs219426	0.6	6.35E-010	3.51E-010	4.71E-001	1.40E-001	1.35E-010
13	rs1131431	rs2195525	-0.54	2.21E-008	4.09E-010	8.30E-001	5.76E-001	1.57E-010
14	rs4697519	rs6120777	-0.55	1.19E-008	4.41E-010	8.83E-001	9.54E-001	5.81E-010
15	rs4912589	rs1822690	-0.59	9.04E-010	4.95E-010	7.61E-001	2.74E-001	6.90E-010
16	rs1423691	rs1109353	-0.56	5.02E-009	5.29E-010	8.93E-001	5.90E-001	5.72E-010
17	rs9548798	rs7257025	-0.55	1.17E-008	5.31E-010	9.66E-001	1.44E-002	9.41E-010
18	rs17290977	rs1360625	-0.57	2.70E-009	5.32E-010	7.81E-001	1.54E-001	7.00E-010
19	rs6802890	rs417704	0.59	1.07E-009	5.62E-010	9.32E-001	4.14E-001	4.97E-010
20	rs1499495	rs12446827	0.59	1.38E-009	5.94E-010	5.10E-001	3.25E-001	4.88E-010
21	rs12155345	rs12683067	-0.57	3.07E-009	6.34E-010	4.37E-001	9.27E-001	7.20E-010
22	rs10494045	rs6771042	-0.57	3.28E-009	6.46E-010	2.83E-001	2.25E-001	5.16E-010
23	rs4915129	rs6771042	-0.57	3.28E-009	6.46E-010	2.83E-001	2.25E-001	5.16E-010
24	rs718224	rs12683067	-0.56	4.63E-009	6.58E-010	6.66E-001	8.69E-001	7.34E-010
25	rs6791266	rs1893814	-0.56	5.71E-009	6.67E-010	6.70E-001	3.33E-001	8.08E-010
26	rs1925338	rs2896569	0.55	1.00E-008	7.20E-010	6.50E-001	3.88E-001	6.79E-010
27	rs2589506	rs7672861	0.56	4.68E-009	7.23E-010	2.50E-001	7.72E-001	8.28E-010
28	rs843622	rs7233189	0.58	2.25E-009	7.35E-010	2.09E-001	3.30E-001	8.91E-010
29	rs1922772	rs1583645	-0.59	1.29E-009	7.37E-010	3.41E-001	2.34E-001	8.86E-010
30	rs938962	rs1725021	-0.56	5.34E-009	7.41E-010	9.76E-001	7.22E-001	8.90E-010
31	rs7761260	rs1005858	-0.6	3.55E-010	7.62E-010	2.75E-001	5.72E-001	1.93E-010
32	rs7761260	rs7111999	-0.61	3.45E-010	8.47E-010	3.22E-001	6.74E-001	2.29E-010
33	rs2300780	rs413946	0.53	3.42E-008	8.70E-010	7.77E-001	1.11E-001	1.04E-009
34	rs6478961	rs2254266	0.52	6.98E-008	9.01E-010	5.50E-002	8.98E-001	1.15E-009

35	rs12046222	rs6771042	-0.57	3.89E-009	9.16E-010	3.99E-001	2.30E-001	7.58E-010
36	rs10518222	rs3777536	0.55	1.48E-008	9.34E-010	1.48E-001	2.61E-001	1.44E-009
37	rs7822757	rs10762351	0.57	4.04E-009	9.40E-010	9.55E-001	5.99E-001	8.96E-010
38	rs17086512	rs2921010	-0.57	3.06E-009	9.67E-010	8.99E-001	1.43E-001	1.12E-009
39	rs7048604	rs598700	-0.58	2.49E-009	1.00E-009	8.01E-001	2.23E-001	9.55E-010
40	rs3930209	rs17255124	0.55	1.17E-008	1.08E-009	1.30E-001	9.73E-001	7.06E-010
41	rs1000291	rs661891	-0.53	3.67E-008	1.12E-009	6.46E-001	4.50E-001	1.22E-009
42	rs6494454	rs4814142	-0.58	1.86E-009	1.12E-009	2.30E-001	3.22E-001	9.25E-010
43	rs938962	rs832984	-0.55	1.07E-008	1.13E-009	9.76E-001	7.71E-001	1.32E-009
44	rs29515	rs12683067	-0.56	5.94E-009	1.20E-009	3.31E-001	8.84E-001	1.23E-009
45	rs12321489	rs2839265	-0.54	2.49E-008	1.24E-009	9.92E-001	7.94E-001	4.88E-010
46	rs12024738	rs2118157	0.56	6.22E-009	1.24E-009	5.85E-001	1.50E-001	1.78E-009
47	rs6737070	rs10401193	0.56	6.06E-009	1.35E-009	5.65E-001	2.88E-001	1.11E-009
48	rs241407	rs213658	-0.52	7.87E-008	1.47E-009	4.34E-001	8.30E-001	3.64E-010
49	rs1518685	rs7899772	-0.57	3.45E-009	1.50E-009	7.00E-001	3.66E-001	1.76E-009
50	rs4654461	rs11625625	-0.54	2.65E-008	1.50E-009	5.57E-001	1.35E-001	1.85E-009
51	rs6965571	rs9933156	0.54	1.86E-008	1.51E-009	1.52E-001	8.73E-003	2.46E-009
52	rs1541084	rs585663	0.58	1.94E-009	1.51E-009	9.70E-001	7.47E-001	2.27E-009
53	rs202963	rs6039459	-0.52	5.55E-008	1.53E-009	4.27E-001	8.03E-001	9.43E-010
54	rs1035630	rs2243399	0.54	2.16E-008	1.57E-009	6.10E-005	4.42E-001	1.66E-009
55	rs12048393	rs9380409	-0.58	1.57E-009	1.57E-009	9.09E-001	8.49E-001	1.95E-009
56	rs9840388	rs1602816	0.54	2.42E-008	1.60E-009	2.06E-001	7.90E-001	1.95E-009
57	rs9356821	rs9294264	0.52	5.95E-008	1.61E-009	7.70E-001	9.28E-001	3.26E-010
58	rs9999979	rs2064317	-0.57	4.17E-009	1.62E-009	9.84E-001	7.94E-001	1.92E-009
59	rs9293756	rs8076149	-0.5	1.67E-007	1.62E-009	6.44E-001	1.32E-001	1.95E-009
60	rs1962363	rs4382270	0.55	1.41E-008	1.68E-009	8.09E-001	6.16E-001	1.72E-009
61	rs1962363	rs9321246	0.55	1.12E-008	1.74E-009	7.62E-001	4.93E-001	1.82E-009
62	rs1523113	rs2540552	0.57	3.91E-009	1.74E-009	3.60E-001	9.72E-001	1.24E-009
63	rs13191198	rs2830204	-0.56	8.86E-009	1.76E-009	5.24E-001	4.14E-001	2.62E-010
64	rs6537355	rs3782294	-0.58	2.07E-009	1.78E-009	2.12E-001	6.90E-001	1.40E-009
65	rs4982032	rs871044	-0.55	1.02E-008	1.85E-009	9.14E-001	7.97E-002	1.76E-009
66	rs12321489	rs2839243	-0.53	5.57E-008	1.86E-009	9.92E-001	9.82E-001	6.28E-010
67	rs7434469	rs11100904	0.55	1.19E-008	1.88E-009	2.05E-001	2.57E-001	1.68E-009
68	rs11942384	rs3019793	-0.53	3.77E-008	1.89E-009	2.86E-001	5.81E-001	1.51E-009
69	rs1263560	rs2160935	-0.55	1.45E-008	1.90E-009	6.67E-001	6.56E-001	2.15E-009
70	rs6737070	rs4808199	0.56	8.30E-009	1.91E-009	5.65E-001	2.11E-001	1.59E-009
71	rs977576	rs375310	0.56	8.69E-009	1.94E-009	8.55E-001	8.83E-001	2.37E-009
72	rs10048926	rs1377392	-0.56	5.14E-009	1.97E-009	8.86E-001	6.41E-001	1.60E-009
73	rs7730720	rs8076149	-0.51	1.33E-007	1.97E-009	5.49E-001	1.60E-001	2.35E-009

74	rs725703	rs6771042	-0.57	3.47E-009	1.99E-009	1.26E-001	2.38E-001	1.41E-009
75	rs7653262	rs516783	0.53	3.36E-008	2.00E-009	3.82E-001	3.19E-003	1.72E-009
76	rs1978910	rs288980	-0.55	1.44E-008	2.10E-009	8.91E-001	4.61E-001	1.27E-009
77	rs6657655	rs425203	0.51	9.22E-008	2.12E-009	5.89E-001	6.06E-001	2.52E-009
78	rs4291539	rs138150	-0.55	1.10E-008	2.13E-009	8.47E-001	3.72E-001	2.34E-009
79	rs188904	rs737654	0.53	3.40E-008	2.21E-009	5.84E-001	3.91E-001	2.59E-009
80	rs7681365	rs2367430	0.55	9.98E-009	2.21E-009	3.13E-001	3.52E-001	8.88E-010
81	rs7048604	rs1410810	0.56	8.57E-009	2.27E-009	8.01E-001	1.12E-001	1.60E-009
82	rs7048604	rs1535532	0.56	8.57E-009	2.27E-009	8.01E-001	1.12E-001	1.60E-009
83	rs6730381	rs4141130	-0.54	2.75E-008	2.29E-009	9.02E-001	9.81E-002	2.09E-009
84	rs12321489	rs13373028	-0.52	6.99E-008	2.30E-009	9.92E-001	9.31E-001	7.55E-010
85	rs153252	rs211409	0.53	4.79E-008	2.30E-009	8.43E-001	9.67E-001	1.37E-009
86	rs1041205	rs8013347	0.56	4.78E-009	2.31E-009	6.23E-001	6.71E-002	2.35E-009
87	rs291538	rs676466	-0.55	1.67E-008	2.38E-009	2.30E-003	6.14E-001	1.71E-009
88	rs4307594	rs11984755	-0.52	5.57E-008	2.39E-009	9.73E-001	9.33E-001	1.92E-009
89	rs1397726	rs959167	0.53	4.41E-008	2.39E-009	3.65E-001	6.73E-002	1.42E-009
90	rs2894960	rs2282522	0.51	1.09E-007	2.40E-009	4.57E-001	2.65E-001	2.33E-009
91	rs1721105	rs6990663	-0.57	4.78E-009	2.40E-009	4.57E-001	3.33E-002	1.36E-009
92	rs2037204	rs9663932	-0.6	5.62E-010	2.43E-009	4.59E-001	7.35E-001	6.61E-010
93	rs4890882	rs2327206	-0.55	1.10E-008	2.45E-009	6.47E-002	6.43E-001	1.19E-009
94	rs2260697	rs261227	0.56	6.74E-009	2.47E-009	8.88E-001	9.32E-001	2.74E-009
95	rs13064262	rs4975625	0.52	8.46E-008	2.50E-009	9.11E-001	3.50E-001	2.83E-009
96	rs2250806	rs7545182	0.53	3.52E-008	2.51E-009	2.08E-001	8.77E-001	3.99E-009
97	rs3861866	rs1662694	0.58	1.82E-009	2.52E-009	3.46E-001	7.71E-001	3.36E-009
98	rs3861866	rs333917	0.58	1.82E-009	2.52E-009	3.46E-001	7.71E-001	3.36E-009
99	rs2504805	rs4369386	0.53	5.03E-008	2.52E-009	5.72E-002	3.41E-001	4.82E-009
100	rs6597753	rs30405	-0.55	1.20E-008	2.56E-009	1.88E-002	4.47E-001	4.04E-009

Table S.2 Top 100 Multiple sclerosis SNP pairs ranked by FastEpistasis

Rank	SNP1 Name	SNP2 Name	Diff. of R	Diff. Of R Pvalue	FastEpistatic Pvalue	Lreg-SNP1 Pvalue	Lreg-SNP2 Pvalue	Lreg-Interaction Pvalue
1	rs4653309	rs17338700	0.61	2.26E-10	6.97E-12	1.94E-01	6.16E-01	8.98E-12
2	rs4984422	rs1967113	-0.66	8.86E-12	1.06E-11	2.02E-01	8.66E-01	4.72E-13
3	rs1156847	rs7246846	0.62	1.21E-10	6.57E-11	7.45E-01	2.01E-01	4.02E-11
4	rs6455842	rs265548	0.64	2.81E-11	7.25E-11	3.67E-01	3.55E-01	6.17E-12
5	rs12188192	rs1317584	0.58	1.98E-09	8.08E-11	2.51E-01	4.90E-01	1.87E-10
6	rs2100807	rs4875302	0.61	1.95E-10	1.88E-10	7.15E-01	3.95E-01	1.45E-10
7	rs11900448	rs11939830	-0.6	5.07E-10	2.17E-10	2.27E-01	7.97E-01	2.64E-10
8	rs6762261	rs4745430	0.61	3.24E-10	2.36E-10	4.81E-01	1.87E-01	1.65E-10
9	rs2374344	rs1011308	0.55	1.26E-08	2.53E-10	3.97E-01	4.00E-01	4.41E-10
10	rs11925795	rs4731772	0.62	1.60E-10	3.11E-10	3.49E-03	4.37E-01	4.71E-10
11	rs1001763	rs1584407	0.56	5.77E-09	3.31E-10	4.32E-01	2.92E-01	1.86E-10
12	rs7776948	rs219426	0.6	6.35E-10	3.51E-10	4.71E-01	1.40E-01	1.35E-10
13	rs1131431	rs2195525	-0.54	2.21E-08	4.09E-10	8.30E-01	5.76E-01	1.57E-10
14	rs4697519	rs6120777	-0.55	1.19E-08	4.41E-10	8.83E-01	9.54E-01	5.81E-10
15	rs4912589	rs1822690	-0.59	9.04E-10	4.95E-10	7.61E-01	2.74E-01	6.90E-10
16	rs1423691	rs1109353	-0.56	5.02E-09	5.29E-10	8.93E-01	5.90E-01	5.72E-10
17	rs9548798	rs7257025	-0.55	1.17E-08	5.31E-10	9.66E-01	1.44E-02	9.41E-10
18	rs17290977	rs1360625	-0.57	2.70E-09	5.32E-10	7.81E-01	1.54E-01	7.00E-10
19	rs6802890	rs417704	0.59	1.07E-09	5.62E-10	9.32E-01	4.14E-01	4.97E-10
20	rs1499495	rs12446827	0.59	1.38E-09	5.94E-10	5.10E-01	3.25E-01	4.88E-10
21	rs12155345	rs12683067	-0.57	3.07E-09	6.34E-10	4.37E-01	9.27E-01	7.20E-10
22	rs10494045	rs6771042	-0.57	3.28E-09	6.46E-10	2.83E-01	2.25E-01	5.16E-10
23	rs4915129	rs6771042	-0.57	3.28E-09	6.46E-10	2.83E-01	2.25E-01	5.16E-10
24	rs718224	rs12683067	-0.56	4.63E-09	6.58E-10	6.66E-01	8.69E-01	7.34E-10
25	rs6791266	rs1893814	-0.56	5.71E-09	6.67E-10	6.70E-01	3.33E-01	8.08E-10
26	rs1925338	rs2896569	0.55	1.00E-08	7.20E-10	6.50E-01	3.88E-01	6.79E-10
27	rs2589506	rs7672861	0.56	4.68E-09	7.23E-10	2.50E-01	7.72E-01	8.28E-10
28	rs843622	rs7233189	0.58	2.25E-09	7.35E-10	2.09E-01	3.30E-01	8.91E-10
29	rs1922772	rs1583645	-0.59	1.29E-09	7.37E-10	3.41E-01	2.34E-01	8.86E-10
30	rs938962	rs1725021	-0.56	5.34E-09	7.41E-10	9.76E-01	7.22E-01	8.90E-10
31	rs7761260	rs1005858	-0.6	3.55E-10	7.62E-10	2.75E-01	5.72E-01	1.93E-10
32	rs7761260	rs7111999	-0.61	3.45E-10	8.47E-10	3.22E-01	6.74E-01	2.29E-10
33	rs2300780	rs413946	0.53	3.42E-08	8.70E-10	7.77E-01	1.11E-01	1.04E-09
34	rs6478961	rs2254266	0.52	6.98E-08	9.01E-10	5.50E-02	8.98E-01	1.15E-09

35	rs12046222	rs6771042	-0.57	3.89E-09	9.16E-10	3.99E-01	2.30E-01	7.58E-10
36	rs10518222	rs3777536	0.55	1.48E-08	9.34E-10	1.48E-01	2.61E-01	1.44E-09
37	rs7822757	rs10762351	0.57	4.04E-09	9.40E-10	9.55E-01	5.99E-01	8.96E-10
38	rs17086512	rs2921010	-0.57	3.06E-09	9.67E-10	8.99E-01	1.43E-01	1.12E-09
39	rs7048604	rs598700	-0.58	2.49E-09	1.00E-09	8.01E-01	2.23E-01	9.55E-10
40	rs3930209	rs17255124	0.55	1.17E-08	1.08E-09	1.30E-01	9.73E-01	7.06E-10
41	rs1000291	rs661891	-0.53	3.67E-08	1.12E-09	6.46E-01	4.50E-01	1.22E-09
42	rs6494454	rs4814142	-0.58	1.86E-09	1.12E-09	2.30E-01	3.22E-01	9.25E-10
43	rs938962	rs832984	-0.55	1.07E-08	1.13E-09	9.76E-01	7.71E-01	1.32E-09
44	rs29515	rs12683067	-0.56	5.94E-09	1.20E-09	3.31E-01	8.84E-01	1.23E-09
45	rs12321489	rs2839265	-0.54	2.49E-08	1.24E-09	9.92E-01	7.94E-01	4.88E-10
46	rs12024738	rs2118157	0.56	6.22E-09	1.24E-09	5.85E-01	1.50E-01	1.78E-09
47	rs6737070	rs10401193	0.56	6.06E-09	1.35E-09	5.65E-01	2.88E-01	1.11E-09
48	rs241407	rs213658	-0.52	7.87E-08	1.47E-09	4.34E-01	8.30E-01	3.64E-10
49	rs1518685	rs7899772	-0.57	3.45E-09	1.50E-09	7.00E-01	3.66E-01	1.76E-09
50	rs4654461	rs11625625	-0.54	2.65E-08	1.50E-09	5.57E-01	1.35E-01	1.85E-09
51	rs6965571	rs9933156	0.54	1.86E-08	1.51E-09	1.52E-01	8.73E-03	2.46E-09
52	rs1541084	rs585663	0.58	1.94E-09	1.51E-09	9.70E-01	7.47E-01	2.27E-09
53	rs202963	rs6039459	-0.52	5.55E-08	1.53E-09	4.27E-01	8.03E-01	9.43E-10
54	rs1035630	rs2243399	0.54	2.16E-08	1.57E-09	6.10E-05	4.42E-01	1.66E-09
55	rs12048393	rs9380409	-0.58	1.57E-09	1.57E-09	9.09E-01	8.49E-01	1.95E-09
56	rs9840388	rs1602816	0.54	2.42E-08	1.60E-09	2.06E-01	7.90E-01	1.95E-09
57	rs9356821	rs9294264	0.52	5.95E-08	1.61E-09	7.70E-01	9.28E-01	3.26E-10
58	rs9999979	rs2064317	-0.57	4.17E-09	1.62E-09	9.84E-01	7.94E-01	1.92E-09
59	rs9293756	rs8076149	-0.5	1.67E-07	1.62E-09	6.44E-01	1.32E-01	1.95E-09
60	rs1962363	rs4382270	0.55	1.41E-08	1.68E-09	8.09E-01	6.16E-01	1.72E-09
61	rs1962363	rs9321246	0.55	1.12E-08	1.74E-09	7.62E-01	4.93E-01	1.82E-09
62	rs1523113	rs2540552	0.57	3.91E-09	1.74E-09	3.60E-01	9.72E-01	1.24E-09
63	rs13191198	rs2830204	-0.56	8.86E-09	1.76E-09	5.24E-01	4.14E-01	2.62E-10
64	rs6537355	rs3782294	-0.58	2.07E-09	1.78E-09	2.12E-01	6.90E-01	1.40E-09
65	rs4982032	rs871044	-0.55	1.02E-08	1.85E-09	9.14E-01	7.97E-02	1.76E-09
66	rs12321489	rs2839243	-0.53	5.57E-08	1.86E-09	9.92E-01	9.82E-01	6.28E-10
67	rs7434469	rs11100904	0.55	1.19E-08	1.88E-09	2.05E-01	2.57E-01	1.68E-09
68	rs11942384	rs3019793	-0.53	3.77E-08	1.89E-09	2.86E-01	5.81E-01	1.51E-09
69	rs1263560	rs2160935	-0.55	1.45E-08	1.90E-09	6.67E-01	6.56E-01	2.15E-09
70	rs6737070	rs4808199	0.56	8.30E-09	1.91E-09	5.65E-01	2.11E-01	1.59E-09
71	rs977576	rs375310	0.56	8.69E-09	1.94E-09	8.55E-01	8.83E-01	2.37E-09
72	rs10048926	rs1377392	-0.56	5.14E-09	1.97E-09	8.86E-01	6.41E-01	1.60E-09
73	rs7730720	rs8076149	-0.51	1.33E-07	1.97E-09	5.49E-01	1.60E-01	2.35E-09

74	rs725703	rs6771042	-0.57	3.47E-09	1.99E-09	1.26E-01	2.38E-01	1.41E-09
75	rs7653262	rs516783	0.53	3.36E-08	2.00E-09	3.82E-01	3.19E-03	1.72E-09
76	rs1978910	rs288980	-0.55	1.44E-08	2.10E-09	8.91E-01	4.61E-01	1.27E-09
77	rs6657655	rs425203	0.51	9.22E-08	2.12E-09	5.89E-01	6.06E-01	2.52E-09
78	rs4291539	rs138150	-0.55	1.10E-08	2.13E-09	8.47E-01	3.72E-01	2.34E-09
79	rs188904	rs737654	0.53	3.40E-08	2.21E-09	5.84E-01	3.91E-01	2.59E-09
80	rs7681365	rs2367430	0.55	9.98E-09	2.21E-09	3.13E-01	3.52E-01	8.88E-10
81	rs7048604	rs1410810	0.56	8.57E-09	2.27E-09	8.01E-01	1.12E-01	1.60E-09
82	rs7048604	rs1535532	0.56	8.57E-09	2.27E-09	8.01E-01	1.12E-01	1.60E-09
83	rs6730381	rs4141130	-0.54	2.75E-08	2.29E-09	9.02E-01	9.81E-02	2.09E-09
84	rs12321489	rs13373028	-0.52	6.99E-08	2.30E-09	9.92E-01	9.31E-01	7.55E-10
85	rs153252	rs211409	0.53	4.79E-08	2.30E-09	8.43E-01	9.67E-01	1.37E-09
86	rs1041205	rs8013347	0.56	4.78E-09	2.31E-09	6.23E-01	6.71E-02	2.35E-09
87	rs291538	rs676466	-0.55	1.67E-08	2.38E-09	2.30E-03	6.14E-01	1.71E-09
88	rs4307594	rs11984755	-0.52	5.57E-08	2.39E-09	9.73E-01	9.33E-01	1.92E-09
89	rs1397726	rs959167	0.53	4.41E-08	2.39E-09	3.65E-01	6.73E-02	1.42E-09
90	rs2894960	rs2282522	0.51	1.09E-07	2.40E-09	4.57E-01	2.65E-01	2.33E-09
91	rs1721105	rs6990663	-0.57	4.78E-09	2.40E-09	4.57E-01	3.33E-02	1.36E-09
92	rs2037204	rs9663932	-0.6	5.62E-10	2.43E-09	4.59E-01	7.35E-01	6.61E-10
93	rs4890882	rs2327206	-0.55	1.10E-08	2.45E-09	6.47E-02	6.43E-01	1.19E-09
94	rs2260697	rs261227	0.56	6.74E-09	2.47E-09	8.88E-01	9.32E-01	2.74E-09
95	rs13064262	rs4975625	0.52	8.46E-08	2.50E-09	9.11E-01	3.50E-01	2.83E-09
96	rs2250806	rs7545182	0.53	3.52E-08	2.51E-09	2.08E-01	8.77E-01	3.99E-09
97	rs3861866	rs1662694	0.58	1.82E-09	2.52E-09	3.46E-01	7.71E-01	3.36E-09
98	rs3861866	rs333917	0.58	1.82E-09	2.52E-09	3.46E-01	7.71E-01	3.36E-09
99	rs2504805	rs4369386	0.53	5.03E-08	2.52E-09	5.72E-02	3.41E-01	4.82E-09
100	rs6597753	rs30405	-0.55	1.20E-08	2.56E-09	1.88E-02	4.47E-01	4.04E-09